

# The right choice matters!

SMT solving substantially improves  
model-based debugging of spreadsheets.

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# Fault Localization in Spreadsheets

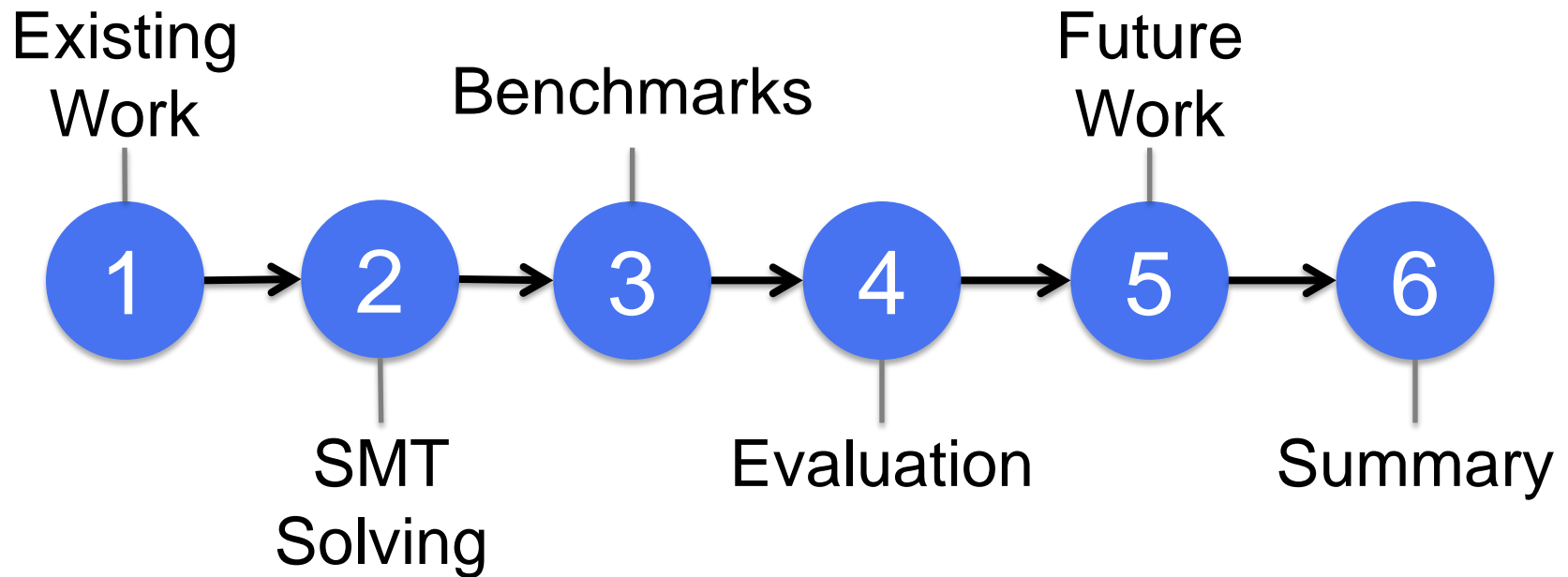
- What is Spreadsheet fault localization?
- Why important?
  - Spreadsheet users outnumber programmers
  - Basis for decisions, but error prone
  - Hard to debug spreadsheets
- Attempts to use model-based debugging

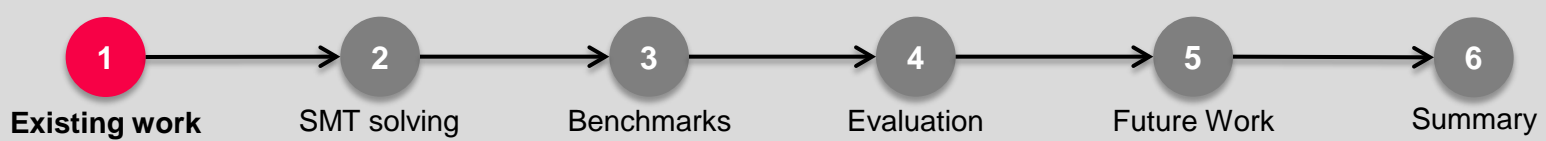
Limitations

→ No support for real numbers

→ Solving time

# Outline





## Existing work

- Abreu et al.: “Constraint-based Debugging of Spreadsheets” [ARW12]  
**Minion constraint solver**
- Jannach and Engler: “Toward model-based debugging of spreadsheet programs” [JE10]  
**Choco constraint solver**

Limitations  
No Support for Real Numbers  
Solving Time

[ARW12] Rui Abreu, André Riboira, and Franz Wotawa. “Constraint-based Debugging of Spreadsheets.” 15<sup>th</sup> Iberoamerican Conference on Software Engineering, 2012, pp. 1–14.

[JE10] Dietmar Jannach and Ulrich Engler. “Toward model-based debugging of spreadsheet programs.” 9<sup>th</sup> Joint Conference on Knowledge-Based Software Engineering 2010, pp. 252–264.

# Running Example

## Faulty Spreadsheet

|   | A            | B             | C             | D            | E           | F                |
|---|--------------|---------------|---------------|--------------|-------------|------------------|
| 1 |              | <b>week 1</b> | <b>week 2</b> | <b>Total</b> | <b>\$/h</b> | <b>Gross Pay</b> |
| 2 | Green        | 23            | 31            | 23           | 15          | \$345,00         |
| 3 | Jones        | 35            | 34            | 69           | 17          | \$1.173,00       |
| 4 | <b>Total</b> | 58            | 65            | 92           |             |                  |

## Formula View

|   | A            | B             | C             | D            | E           | F                |
|---|--------------|---------------|---------------|--------------|-------------|------------------|
| 1 |              | <b>week 1</b> | <b>week 2</b> | <b>Total</b> | <b>\$/h</b> | <b>Gross Pay</b> |
| 2 | Green        | 23            | 31            | =SUM(B2)     | 15          | =D2*E2           |
| 3 | Jones        | 35            | 34            | =SUM(B3:C3)  | 17          | =D3*E3           |
| 4 | <b>Total</b> | =SUM(B2:B3)   | =SUM(C2:C3)   | =SUM(D2:D3)  |             |                  |

Source: EUSES Spreadsheet Corpus

# Test Cases for Spreadsheets

- **Input cells:** cells that do not reference other cells

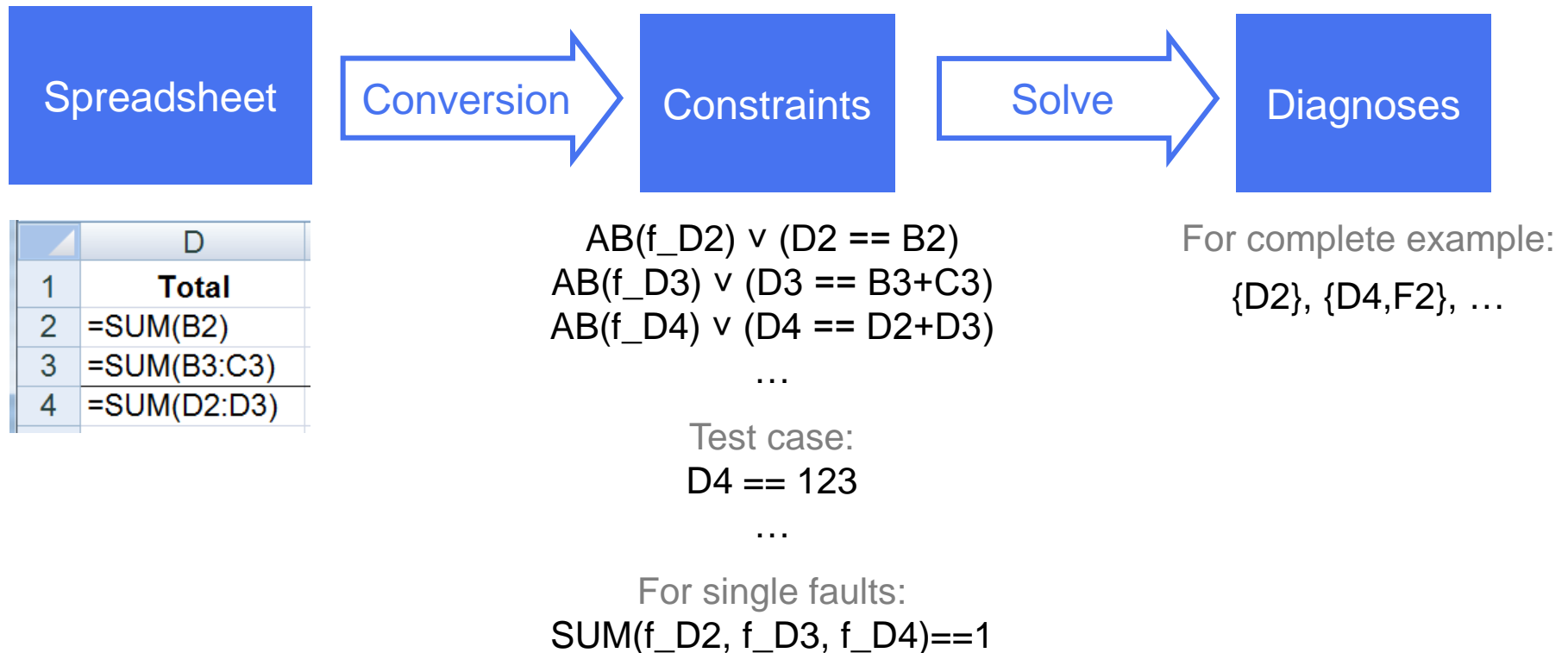
$I = \{B2=23, C2=31, E2=15, B3=35, C3=34, E3=17\}$

- **Output cells:** any formula cell, determined by user

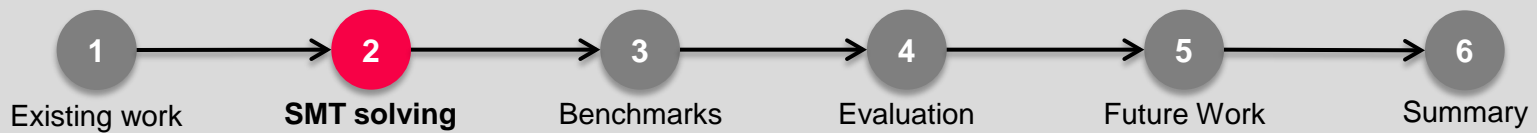
$O = \{B4=58, C4=65, D4=123, F2=810, F3=1173\}$

|   | A            | B             | C             | D            | E           | F                |
|---|--------------|---------------|---------------|--------------|-------------|------------------|
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# Constraint-based Debugging (ConBug)



[ARW12] Rui Abreu, André Riboira, and Franz Wotawa. "Constraint-based Debugging of Spreadsheets." 15<sup>th</sup> Iberoamerican Conference on Software Engineering, 2012, pp. 1–14.



# Satisfiability modulo theories (SMT) solver

- Based on Boolean satisfiability
- Enhanced by different theories (e.g. Integer, Real)
- Solves decision problem
  - Determine diagnoses via MCSes and MCSes-U algorithms [LS08, LS09]
- Z3 solver
  - Speedup in computation time
  - Handling of real numbers

[LS08] M. H. Liffiton and K. A. Sakallah. “Algorithms for computing minimal unsatisfiable subsets of constraints,” *J. Autom. Reason.*, vol. 40, no. 1, pp. 1–33, Jan. 2008.

[LS09] M. H. Liffiton and K. A. Sakallah. “Generalizing core-guided max-sat,” 12th Int. Conference on Theory and Applications of Satisfiability Testing (SAT '09). Springer-Verlag, 2009, pp. 481–494.





## Spreadsheet Corpora (1)

- Limitations of EUSES spreadsheet corpus [FR05]
  - Many small spreadsheets
  - Missing input values
  - Obsolete file formats
  - No faulty versions

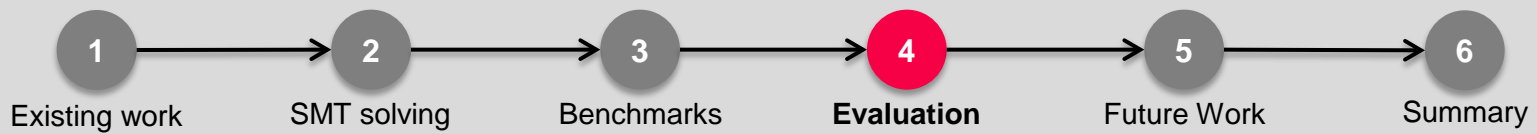
[FR05] Marc II Fisher and Gregg Rothermel. “The EUSES Spreadsheet Corpus: A Shared Resource for Supporting Experimentation with Spreadsheet Dependability Mechanisms.” 1st Workshop on End-User Software Engineering. 2005, pp. 47–51.



## Spreadsheet Corpora (2)

|                   |  |  |
|-------------------|--|--|
|                   | Mod. EUSES corpus  | Integer corpus                               |
| <b>Source</b>     | Filtering from EUSES   | Artificially created + existing spreadsheets |
| <b>Domain</b>     | Reals  | Integer                                      |
| <b>Mutants</b>    | 622 mutants<br><i>created with spreadsheet mutation operators [AE09]</i> | 220 mutants                                  |
| <b>Complexity</b> | 6 to 4,000 formulas<br>AVG: 225 formulas                                 | 7 to 233 formulas<br>AVG: 39 formulas        |

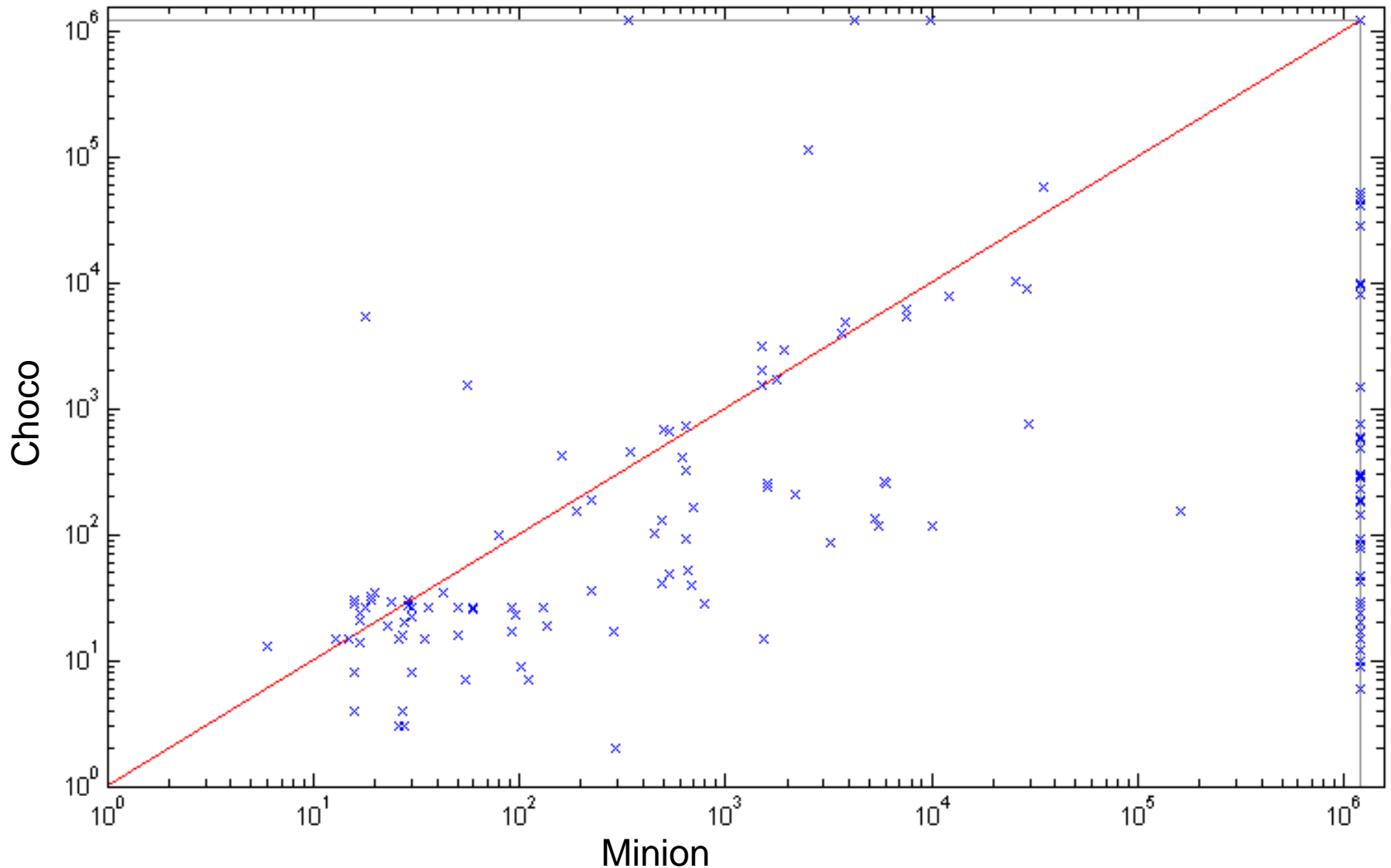
Original spreadsheets + mutants publicly available



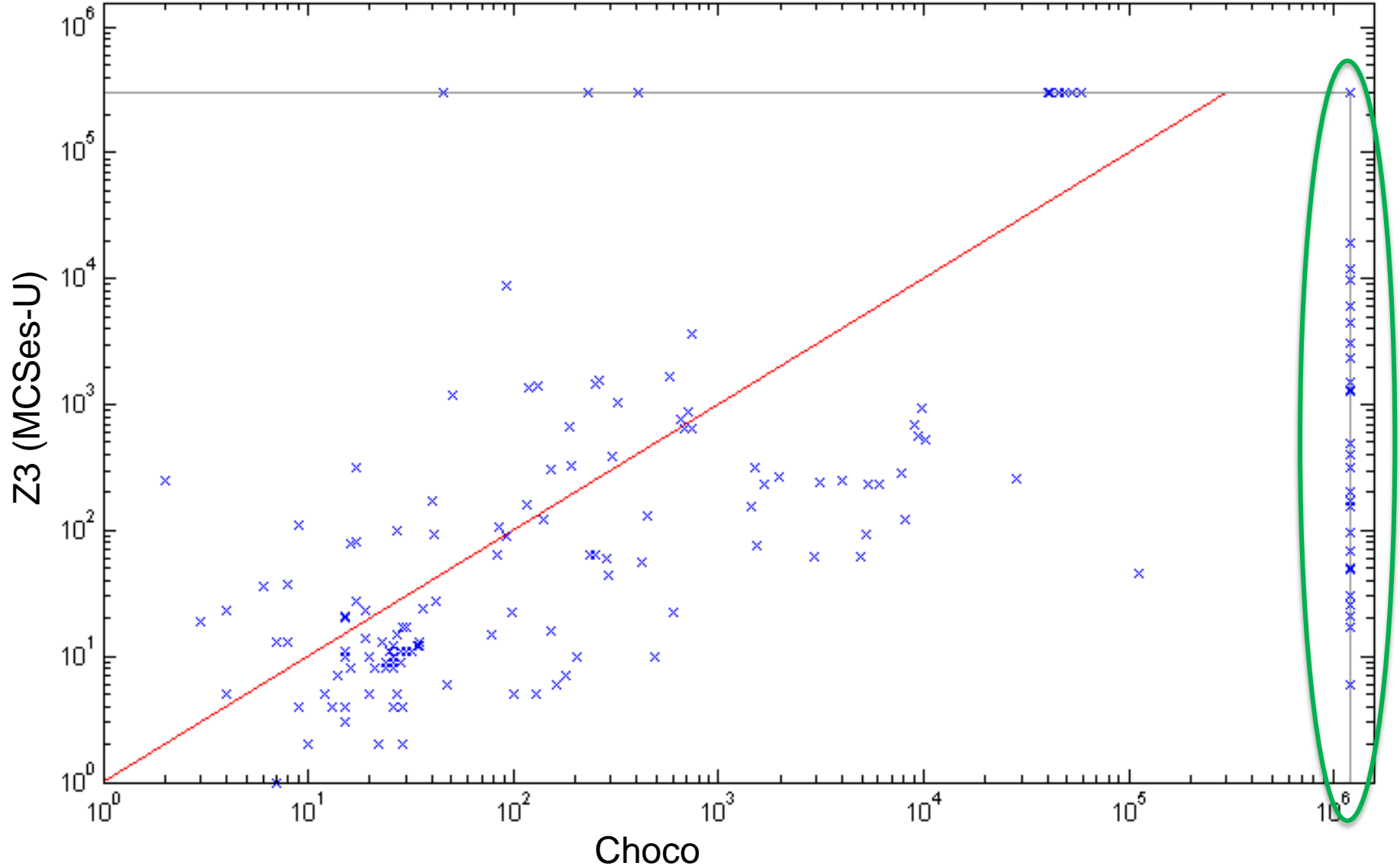
# Empirical Evaluation

- Runtime comparison
  - Minion vs. Choco vs. Z3 (MCSes and MCSes-U)  
Integer corpus
  - Integers vs. Real numbers  
Integer corpus + Real number version
- Reduction quality
  - Modified EUSES corpus

# Runtime comparison [in ms]: Choco vs. Minion



# Runtime comparison [in ms]: Z3 vs. Choco



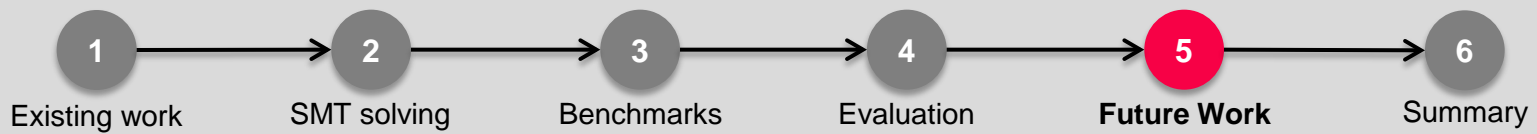
# Detailed runtime comparison

- Choco slightly faster than Minion
- Z3 faster than Minion and Choco
  - Approx. 6 times faster for Integer corpus
- Integer vs. Real domain
  - Integer spreadsheets approx. 2.6 times faster than Reals



# Reduction quality

- $\text{Reduction} = 1 - \frac{\text{Cells in diagnoses}}{\text{Formula cells}} \times 100\%$
- Evaluation basis
  - Subset of mod. EUSES corpus
  - 183 of 622 spreadsheets
- Results
  - 12 spreadsheets: timeout 5 minutes
  - ~ 80 % reduction
  - ~ 500 ms avg. solving time (Z3)



# Future Work and Open Challenges

- Scalability problem (Hypertree complexity)
- User interface and user acceptance study
- Explanations for the user (traceability)
- Dealing with vague user input







## Using Z3 as solver ...

... makes it possible to use model-based debugging for spreadsheets

- In practice (Real numbers) and
- For interactive debugging (Solving time)

